# 12. Heron's Formula

## Exercise 12.1

### 1. Question

Find the area of a triangle whose sides are respectively 150 cm, 120 cm, and 200 cm.

#### Answer

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

$$A = \sqrt{s(s-a)(s-b)(s-c)} \text{ where } s = \frac{a+b+c}{2} \text{ [Heron's Formula]}$$

$$a = 150, b = 120, c = 200$$

$$s = \frac{a+b+c}{2} = \frac{150+120+200}{2} = 235$$

$$A = \sqrt{235(235-150)(235-120)(235-200)}$$

$$A = \sqrt{235\times85\times115\times35} = 25\sqrt{47\times17\times23\times7} = 25\sqrt{128369} \text{ cm}^2$$

#### 2. Question

Find the area of a triangle whose sides are 9 cm, 12 cm and 15 cm.

### Answer

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $a = 9, b = 12, c = 15$   
 $s = \frac{a+b+c}{2} = \frac{9+12+15}{2} = 18$   
A =  $\sqrt{18(18-9)(18-12)(18-15)}$   
A =  $\sqrt{18\times9\times6\times3} = 54$  cm<sup>2</sup>

#### 3. Question

Find the area of a triangle two sides of which are 18 cm and 10 cm and the perimeter is 42 cm.

#### Answer

Let the third side of the triangle is  $\chi$ 

Since the perimeter of a triangle is given by:

a + b + c = perimeter

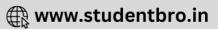
18 + 10 + x = 42

$$x = 42 - 28$$

$$x = 14 \text{ cm}$$

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $a = 18, b = 10, c = 14$   
 $s = \frac{a+b+c}{2} = \frac{18+10+14}{2} = 21$ 



 $A = \sqrt{21(21 - 18)(21 - 10)(21 - 14)}$ 

 $A = \sqrt{21 \times 3 \times 11 \times 7} = 21 \sqrt{11} \text{ cm}^2$ 

### 4. Question

In a  $\triangle$  ABC, AB = 15 cm, BC = 13 cm and AC = 14 cm. Find the area of  $\triangle ABC$  and hence its altitude on AC.

#### Answer

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $a = 15, b = 13, c = 14$   
 $s = \frac{a+b+c}{2} = \frac{15+13+14}{2} = 21$   
A =  $\sqrt{21(21-15)(21-13)(21-14)}$   
A =  $\sqrt{21\times6\times8\times7} = 84$  cm<sup>2</sup>  
Area of triangle =  $\frac{1}{2}$  (*Base*×*Altitude*)  
 $84 = \frac{1}{2}(14\times Altitude)$   
Altitude = 12 cm

#### 5. Question

The perimeter of a triangular field is 540 m and its sides are in the ratio 25 : 17 : 12. Find the area of a triangle.

#### Answer

Sides of the triangle are in ratio: 25: 17: 12

$$a = 25x, b = 17x, c = 12x$$

Since the perimeter of a triangle is given by:

a + b + c = perimeter

25x + 17x + 12x = 540

$$x = \frac{540}{54} = 10$$

Therefore sides of the triangle are:

$$a = 25x = 25 \times 10 = 250$$
,

$$b = 17x = 17 \times 10 = 170$$
,

$$c = 12x = 12 \times 10 = 120$$

When a, b and c are the sides of the triangle and s is the semiperimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2} = \frac{250+170+120}{2} = 270$   
A =  $\sqrt{270(270-250)(270-170)(270-120)}$   
A =  $\sqrt{270(270-250)(270-170)(270-120)}$ 



### 6. Question

The perimeter of a triangle is 300 m. If its sides are in the ratio 3 : 5 : 7. Find the area of the triangle.

#### Answer

Sides of triangle are in ratio: 3:5:7

a = 3x, b = 5x, c = 7x

Since the perimeter of a triangle is given by:

a + b + c = perimeter

3x + 5x + 7x = 300

$$x = \frac{300}{15} = 20$$

$$x = 20$$

Therefore sides of the triangle are:

 $a = 3x = 3 \times 20 = 60$ ,

 $b = 5x = 5 \times 20 = 100$ ,

$$c = 7x = 7 \times 20 = 140$$

When a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

$$A = \sqrt{s(s-a)(s-b)(s-c)} \text{ where } s = \frac{a+b+c}{2} \text{ [Heron's Formula]}$$

$$s = \frac{a+b+c}{2} = \frac{60+100+140}{2} = 150$$

$$A = \sqrt{150(150-60)(150-100)(150-140)}$$

$$A = \sqrt{150\times90\times50\times10} = \sqrt{15\times9\times5\times10000} = \sqrt{15\times3\times3\times5\times10000}$$

$$= \sqrt{15\times3\times15\times10000} = 15\times100\sqrt{3} = 1500\sqrt{3} m^2$$

#### 7. Question

The perimeter of a triangular field is 240 dm. If two of its sides are 78 dm and 50 dm, find the length of the perpendicular on the side of length 50 dm from the opposite vertex.

#### Answer

Let the third side of the triangle is  $\chi$ 

Since the perimeter of a triangle is given by:

a + b + c = perimeter

78 + 50 + x = 240

x = 240 - 128

x = 112 dm

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

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A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $a = 78, b = 50, c = 112$   
 $s = \frac{a+b+c}{2} = \frac{78+50+112}{2} = 120$ 

 $A = \sqrt{120(120 - 78)(120 - 50)(120 - 112)}$ 

 $A = \sqrt{120 \times 42 \times 70 \times 8} = 1680 \text{ dm}^2$ 

Area of triangle =  $\frac{1}{2}(Base \times Altitude)$ 

 $1680 = \frac{1}{2}(50 \times Altitude)$ 

Altitude = 67.2 dm

#### 8. Question

A triangle has sides 35 cm, 54 cm and 61 cm long. Find its area. Also, find the smallest of its altitudes.

#### Answer

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

$$A = \sqrt{s(s-a)(s-b)(s-c)} \text{ where } s = \frac{a+b+c}{2} \text{ [Heron's Formula]}$$

$$a = 35, b = 54, c = 61$$

$$s = \frac{a+b+c}{2} = \frac{35+54+61}{2} = 75$$

$$A = \sqrt{75(75-35)(75-54)(75-61)}$$

$$A = \sqrt{75\times40\times21\times14} = 939.15 \text{ cm}^2$$
Altitude on side 35 cm:  
Area of triangle =  $\frac{1}{2}(Base \times Altitude)$   
939.15 =  $\frac{1}{2}(35 \times Altitude)$   
Altitude = 53.66 cm  
Altitude on side 54 cm:  
Area of triangle =  $\frac{1}{2}(Base \times Altitude)$   
939.15 =  $\frac{1}{2}(54 \times Altitude)$   
Altitude = 34.78 cm  
Altitude on side 61 cm:  
Area of triangle =  $\frac{1}{2}(Base \times Altitude)$   
939.15 =  $\frac{1}{2}(61 \times Altitude)$ 

Altitude = 30.79 cm

Therefore smallest Altitude is: 30.79 cm

#### 9. Question

The lengths of the sides of a triangle are in the ratio 3:4:5 and its perimeter is 144 cm. Find the area of the triangle and the height corresponding to the longest side.

### Answer

Sides of triangle are in ratio: 3:4:5

a = 3x, b = 4x, c = 5x

Since the perimeter of a triangle is given by:





a + b + c = perimeter

3x + 4x + 5x = 144 $x = \frac{144}{12} = 12$ x = 12

Therefore sides of the triangle are:

 $a = 3x = 3 \times 12 = 36,$   $b = 4x = 4 \times 12 = 48,$  $c = 5x = 5 \times 12 = 60$ 

When a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2} = \frac{36+48+60}{2} = 72$   
A =  $\sqrt{72(72-36)(72-48)(72-60)}$   
A =  $\sqrt{72\times36\times24\times12} = 864$  cm<sup>2</sup>  
Area of triangle =  $\frac{1}{2}$  (Base×Altitude)  
 $864 = \frac{1}{2}$  (60×Altitude)

Altitude = 28.8 cm

#### 10. Question

The perimeter of an isosceles triangle is 42 cm and its base is (3/2) times each of the equal sides. Find the length of each side of the triangle, area of the triangle and the height of the triangle.

#### Answer

Let the equal sides of isosceles triangle is  $\chi$ 

Base of the triangle =  $\frac{3x}{2}$ 

Since the perimeter of a triangle is given by:

a + b + c = perimeter

$$x + x + \frac{3x}{2} = 42$$

$$(2x + 2x + 3x)\frac{1}{2} = 42$$

$$x = 12 \text{ cm}$$

Therefore sides of triangle are: a = x = 12, b = x = 12,  $c = \frac{3x}{2} = 18$ 

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

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A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $a = 12, b = 12, c = 18$   
 $s = \frac{a+b+c}{2} = \frac{12+12+18}{2} = 21$ 

 $A = \sqrt{21(21 - 12)(21 - 12)(21 - 18)}$ 

 $A = \sqrt{21 \times 9 \times 9 \times 3} = 71.43 \text{ cm}^2$ 

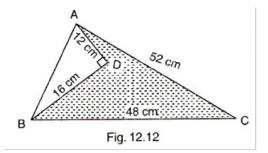
Area of triangle =  $\frac{1}{2}(Base \times Altitude)$ 

 $71.43 = \frac{1}{2}(18 \times Altitude)$ 

Altitude = 7.93 cm

## 11. Question

Find the area os the shaded region in Fig. 12.12.



#### Answer

In right triangle ADB side  $(AB)^2 = (AD)^2 + (BD)^2$ 

 $(AB)^2 = (12)^2 + (16)^2$ 

 $AB = \sqrt{(12)^2 + (16)^2}$ 

 $AB = \sqrt{144 + 256} = 20 \text{ cm}$ 

In right triangle ADB

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $a = 12, b = 16, c = 20$   
 $s = \frac{a+b+c}{2} = \frac{12+16+20}{2} = 24$   
A<sub>1</sub> =  $\sqrt{24(24-12)(24-16)(24-20)}$   
A<sub>1</sub> =  $\sqrt{24\times12\times8\times4} = 96$  cm<sup>2</sup>

In right triangle ABC

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

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$$A_{2} = \sqrt{s(s-a)(s-b)(s-c)} \text{ where } s = \frac{a+b+c}{2}$$

$$a = 20, b = 48, c = 52$$

$$s = \frac{a+b+c}{2} = \frac{20+48+52}{2} = 60$$

$$A_{2} = \sqrt{60(60-20)(60-48)(60-52)}$$

$$A_{2} = \sqrt{60\times40\times12\times8} = 480 \text{ cm}^{2}$$

Area of shaded region is  $A_2$ - $A_1$  = 480 - 96 = 384 cm<sup>2</sup>

## Exercise 12.2

### 1. Question

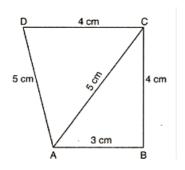
Find the area of a quadrilateral *ABCD* is which AB = 3 cm, BC = 4 cm, CD = 4 cm, DA = 5 cm and AC = 5 cm.

### Answer

Let consider a quadrilateral ABCD

In ΔABC;

AB = a = 3 cm, BC = b = 4 cm, AC = c = 5 cm



Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  $s = \frac{a+b+c}{2} = \frac{3+4+5}{2} = 6$ A<sub>1</sub> =  $\sqrt{6(6-3)(6-4)(6-5)}$ A<sub>1</sub> =  $\sqrt{6\times3\times2\times1} = 6$  cm<sup>2</sup> In  $\Delta$ ADC; DA = a = 5 cm, CD = 4 = 4cm, AC = c = 5 cm Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$   
 $s = \frac{a+b+c}{2} = \frac{5+4+5}{2} = 7$   
A<sub>2</sub> =  $\sqrt{7(7-5)(7-4)(7-5)}$   
A<sub>2</sub> =  $\sqrt{7 \times 2 \times 3 \times 2} = 9.16 \text{ cm}^2$ 

Therefore area of quadrilateral ABCD =  $A_1 + A_2 = 6+9.16 = 15.16 \text{ cm}^2$ 

### 2. Question

The sides of a quadrangular field, taken in order are 26 m, 27 m, 7 m, are 24 m respectively. The angle contained by the last two sides is a right angle. Find its area.

### Answer

Let consider a quadrilateral ABCD

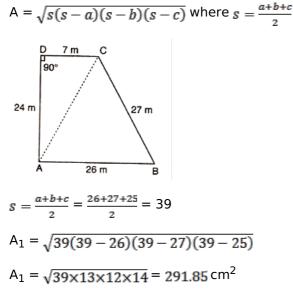
In ΔADC;

 $AC = \sqrt{(24)^2 + 7^2} = 25 \text{ cm}$ 



#### In **ΔABC**

AB = a = 26 cm, BC = b = 27 cm, AC = c = 25 cm Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:



In ΔADC;

DA = a = 24 cm, CD = b = 7cm, AC = c = 25 cm

Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2} = \frac{24+7+25}{2} = 28$   
A<sub>2</sub> =  $\sqrt{28(28-24)(28-7)(28-25)}$   
A<sub>2</sub> =  $\sqrt{28\times4\times21\times3} = 84$  cm<sup>2</sup>

Therefore area of quadrilateral ABCD =  $A_1 + A_2 = 291.85 + 84 = 375.85 \text{ cm}^2$ 

#### 3. Question

The sides of a quadrilateral, taken in order are 5, 12, 14 and 15 metres respectively, and the angle contained by the first two sides is a right angle. Find its area.

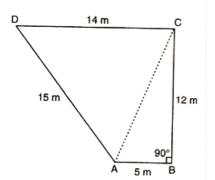
#### Answer

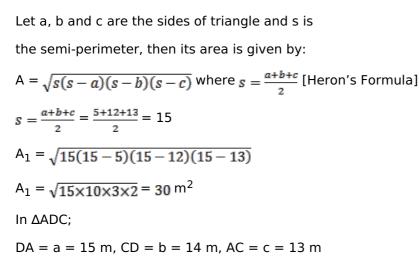
Let consider a quadrilateral ABCD

In ∆ABC;

AC =  $\sqrt{5^2 + (12)^2} = 13 \text{ m}$ AB = a = 5 m, BC = b = 12 m, AC = c = 13 m







Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$   
 $s = \frac{a+b+c}{2} = \frac{15+14+13}{2} = 21$   
A<sub>2</sub> =  $\sqrt{21(21-15)(21-14)(21-13)}$   
A<sub>2</sub> =  $\sqrt{21\times6\times7\times8} = 84 \text{ m}^2$ 

Therefore area of quadrilateral ABCD =  $A_1 + A_2 = 30+84 = 114 \text{ m}^2$ 

#### 4. Question

A park, in the shape of a quadrilateral *ABCD*, has  $C=90^{\circ}$ , AB = 9 m, BC = 12 m, CD = 5 m and AD = 8 m. How much area does it occupy?

#### Answer

Let consider a quadrilateral ABCD

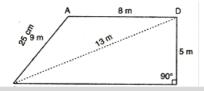
In ΔBCD;

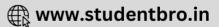
 $BD = \sqrt{(12)^2 + 5^2} = 13 \text{ m}$ 

BC = a = 12 m, CD = b = 5 m, BD = c = 13 m

Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:





A =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  $s = \frac{a+b+c}{2} = \frac{12+5+13}{2} = 15$ A<sub>1</sub> =  $\sqrt{15(15-12)(15-5)(15-13)}$ A<sub>1</sub> =  $\sqrt{15\times3\times10\times2} = 30 \text{ m}^2$ In  $\triangle ABD$ ; AB = a = 9 m, AD = b = 8 m, BD = c = 13 m

AB = a = 3 m, AB = b = 0 m, BB = C = 13

Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$   
 $s = \frac{a+b+c}{2} = \frac{9+8+13}{2} = 15$   
A<sub>2</sub> =  $\sqrt{15(15-9)(15-8)(15-13)}$   
A<sub>2</sub> =  $\sqrt{15\times6\times7\times2} = 35.50 \text{ m}^2$ 

Therefore area of quadrilateral ABCD =  $A_1 + A_2 = 30+35.50 = 65.50 \text{ m}^2$ 

#### 5. Question

Two parallel side of a trapezium are 60 cm and 77 cm and other sides are 25 cm and 26 cm. Find the area of the trapezium.

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#### Answer

Let ABCD is a trapezium in which AB = 77 cm, BC = 26 cm, CD = 60 cm, DA = 25 cm

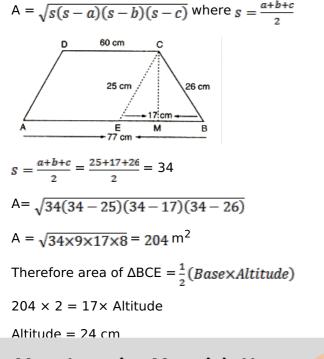
Draw CE// AD

Now, ACDE is a parallelograme

BE = AB-DC = 77-60 = 17 cm

In  $\Delta BEC,$  Let a, b and c are the sides of triangle and

And s be the semi-perimeter, then its area



Area of trapezium ABCD =  $\frac{1}{2}(Sum \ of \ parallel \ sides \times Altitude) = \frac{1}{2}(DC + AB) \times h$ 

$$\Rightarrow \frac{1}{2}(60 + 77) \times 24 = 1644 \ cm^2$$

Therefore area of trapezium ABCD =  $1644 \text{ cm}^2$ 

## 6. Question

Find the area of a rhombus whose perimeter is 80 m and one of whose diagonal is 24 m.

## Answer

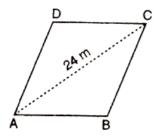
Let ABCD be the rhombus of perimeter 80 m and diagonal AC = 24 m

We have,

AB + BC + CD + DA = 80

4 AB = 80 [:: AB=BC=CD=DA sides of Rhombus]

*AB* = 20 m



In  $\triangle ABC$ , we have

AB = a = 20 cm, BC = b = 20 cm, AC = c = 24 cm

Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  $s = \frac{a+b+c}{2} = \frac{20+20+24}{2} = 32$ A=  $\sqrt{32(32-20)(32-20)(32-24)}$ A =  $\sqrt{32\times12\times12\times8} = 192$  cm<sup>2</sup>

Hence, area of rhombus  $ABCD = 2 \times 192 \text{ m}^2$ 

 $= 384 \text{ m}^2$ 

### 7. Question

A rhombus sheet, whose perimeter is 32 m and whose one diagonal is 10 m long, is painted on both sides at the rate of Rs. 5 per  $m^2$ . Find the cost of painting.

### Answer

Since the sides of a rhombus are equal there fore each side =  $\frac{Perimeter}{4} = \frac{32}{4} = 8 \text{ m}$ 

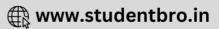
Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]

$$a - \frac{a+b+c}{c} = \frac{8+8+10}{c} = 13$$





 $A = \sqrt{13(13-8)(13-8)(13-10)}$ 

 $A = \sqrt{13 \times 5 \times 5 \times 3} = 31.22 \text{ cm}^2$ 

Hence, area of rhombus  $ABCD = 2 \times 31.22 \text{ m}^2$ 

Total painting area of rhombus =  $62.44 \times 2 = 124.88 \text{ m}^2$ 

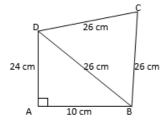
Cost of painting of rhombus on both sides =  $124.88 \times 5 = Rs 624.50$ 

#### 8. Question

Find the area of a quadrilateral *ABCD* in which *AD*= 24 cm, *BAD* = 90° and *BCD* forms an equilateral triangle whose each side is equal to 26 cm. (Take  $\sqrt{3} = 1.73$ )

#### Answer

Let ABCD is a quadrilateral in which AD = 24 cm and  $\Delta$ BCD is an equilateral.



In right angled  $\triangle$ BAD applying pythagorous theorem:

$$(BD)^{2} = (AB)^{2} + (AD)^{2}$$

$$(26)^{2} = (AB)^{2} + (24)^{2}$$

$$\sqrt{676 - 576} = (AB)^{2}$$

$$AB = 10 \text{ cm}$$
Area of right angled  $\Delta BAD = \frac{1}{2}(Base \times Altitude)$ 

$$\Rightarrow \frac{1}{2}(10 \times 24) = 120 \text{ cm}^{2}$$

Now in equilateral △BCD

Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2} = \frac{26+26+26}{2} = 39$ 

 $A = \sqrt{39(39 - 26)(39 - 26)(39 - 26)}$ 

 $A = \sqrt{39 \times 13 \times 13 \times 13} = 292.72 \text{ cm}^2$ 

Hence, area of quad *ABCD* = 120+292.72 =412.72 cm<sup>2</sup>

#### 9. Question

Find the area of a quadrilateral *ABCD* in which AB = 42 cm, BC = 21 cm, CD = 29 cm, DA = 34 cm and diagonal BD = 20 cm.

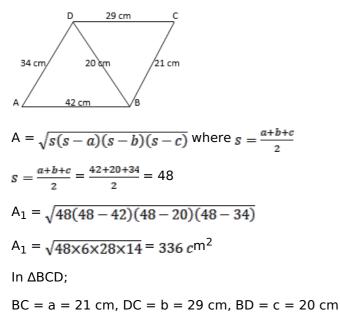
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#### Answer

In ∆ABD;

AB = a = 42 cm, BD = b = 20 cm, DA = c = 34 cm Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:



Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$   
 $s = \frac{a+b+c}{2} = \frac{21+29+20}{2} = 35$   
A<sub>2</sub> =  $\sqrt{35(35-21)(35-29)(35-20)}$   
A<sub>2</sub> =  $\sqrt{35\times14\times6\times15} = 210 \text{ cm}^2$ 

Therefore area of quadrilateral ABCD =  $A_1 + A_2 = 336+210 = 546 \text{ cm}^2$ 

#### 10. Question

Find the perimeter and area of the quadrilateral *ABCD* in which AB = 17 cm, AD = 9 cm, CD = 12 cm,  $ACB = 90^{\circ}$  and AC = 15 cm.

#### Answer

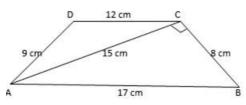
In right  $\triangle$ ACB using pythagorous theorem:

$$(AB)^2 = (AC)^2 + (BC)^2$$

$$(17)^2 = (15)^2 + (BC)^2$$

$$\sqrt{289 - 225} = BC$$

BC = 8 cm



Perimeter of quad ABCD = AB+BC+CD+DA = 17+8+12+9 = 46 cm

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Area of right angled  $\triangle ACB = \frac{1}{2}(Base \times Altitude)$ 

$$\Rightarrow \frac{1}{2}(15 \times 8) = 60 \text{ cm}^2$$

Now in equilateral  $\Delta$ ACD

Let a, b and c are the sides of triangle and s is

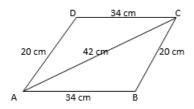
the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2} = \frac{9+12+15}{2} = 18$   
A=  $\sqrt{18(18-9)(18-12)(18-15)}$   
A =  $\sqrt{18\times9\times6\times3} = 54$  cm<sup>2</sup>  
Hence, area of guad *ABCD* = 60+54 = 114 cm<sup>2</sup>

11. Question

The adjacent sides of a parallelogram *ABCD* measure 34 cm and 20 cm, and the diagonal *AC* measures 42 cm. Find the area of the parallelogram.

### Answer



Now in **ΔABC** 

AB = a = 34 cm, BC = b = 20 cm, AC = c = 42 cm

Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$   
 $s = \frac{a+b+c}{2} = \frac{34+20+42}{2} = 48$   
A=  $\sqrt{48(48-34)(48-20)(48-42)}$   
A =  $\sqrt{48\times14\times28\times6} = 336 \text{ cm}^2$ 

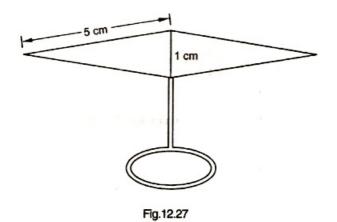
Hence, area of Parallelograme  $ABCD = 2 \times 336 = 672 \text{ cm}^2$ 

## 12. Question

Find the area of the blades of the magnetic compass shown in Fig. 12.27. (Take  $\sqrt{11}$  = 3.32).







#### Answer

Let a, b and c are the sides of blade and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2} = \frac{5+5+1}{2} = 5.5$   
A=  $\sqrt{5.5(5.5-5)(5.5-5)(5.5-1)}$   
A =  $\sqrt{5.5 \times 0.5 \times 0.5 \times 4.5} = 2.49$  cm<sup>2</sup>

Hence, total area of both the blades =  $2 \times 2.49 = 4.98$  cm<sup>2</sup>

#### 13. Question

A hand fan is made by stitching 10 equal size triangular strips of two different types of paper as shown in Fig. 12.28. The dimensions of equal strips are 25 cm, 25 cm and 14 cm. Find the area of each type of paper needed to make the hand fan.

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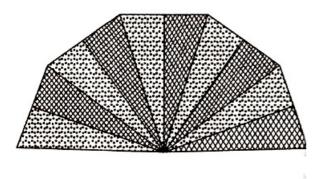


Fig. 12.28

#### Answer

Let a, b and c are the sides of triangular strips and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2} = \frac{25+25+14}{2} = 32$   
A=  $\sqrt{32(32-25)(32-25)(32-14)}$   
A =  $\sqrt{32\times7\times7\times18} = 168$  cm<sup>2</sup>

Hence, total area of 5 Nos of triangular strips of one type =  $5 \times 168 = 840 \text{ cm}^2$ 

#### 14. Question

A triangle and a parallelogram have the same base and the same area. If the sides of the triangle are 13 cm, 14 cm and 15 cm and the parallelogram stands on the base 14 cm, find the height of the parallelpgram.

### Answer

Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  $s = \frac{a+b+c}{2} = \frac{13+14+15}{2} = 21$ A=  $\sqrt{21(21-13)(21-14)(21-15)}$ A =  $\sqrt{21\times8\times7\times6} = 84$  cm<sup>2</sup> Therefore area of  $\Delta = \frac{1}{2}$  (Base×Altitude) 84 × 2 = 14× Altitude Altitude = 12 cm

## **CCE - Formative Assessment**

### 1. Question

Find the area of a triangle whose base and altitude are 5 cm and 4 cm respectively.

### Answer

Base = 5 cm, Altitude = 4 cm Area of  $\Delta = \frac{1}{2}(Base \times Altitude)$ Area of  $\Delta = \frac{1}{2}(5 \times 4) = 10 \text{ cm}^2$ 

### 2. Question

Find the area of a triangle whose sides are 3 cm, 4 cm, and 5 cm respectively.

### Answer

Let a, b and c are the sides of triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]

$$s = \frac{a+b+c}{2} = \frac{3+4+5}{2} = 6$$
$$A = \sqrt{6(6-3)(6-4)(6-5)}$$

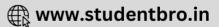
$$A = \sqrt{6 \times 3 \times 2 \times 1} = 6 \text{ cm}^2$$

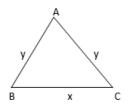
## 3. Question

Find the area of an isosceles triangle having the base  $x \, \text{cm}$  and one side  $y \, \text{cm}$ .

### Answer







In  $\triangle ABC$ , AB = x, BC = x, AC = y .....Given

Since  $\chi$ ,  $\chi$  and  $\gamma$  are the sides of an isosceles triangle and s is

the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{x+y+y}{2} = \frac{x+2y}{2}$   
A=  $\sqrt{\frac{x+2y}{2}(\frac{x+2y}{2}-x)(\frac{x+2y}{2}-y)(\frac{x+2y}{2}-y)}$   
A =  $\sqrt{\frac{x+2y}{2}(\frac{2y-x}{2})(\frac{x}{2})(\frac{x}{2})} = \frac{x}{2}\sqrt{y^2 - \frac{x^2}{4}}$  cm<sup>2</sup>

#### 4. Question

Find the area of an equilateral triangle having each side 4 cm.

#### Answer

Area of an equilateral triangle =  $\frac{\sqrt{3}a^2}{4} = \frac{\sqrt{3}\times4\times4}{4} = 4\sqrt{3} \text{ cm}^2$ 

#### 5. Question

Find the area of an equilateral triangle having each side x cm.

#### Answer

Area of an equilateral triangle  $=\frac{\sqrt{3}a^2}{4}=\frac{\sqrt{3}\times x\times x}{4}=\frac{\sqrt{3}x^2}{4}$  cm<sup>2</sup>

#### 6. Question

The perimeter of a triangular field is 144 m and the ratio of the sides is 3 : 4 : 5. Find the area of the field.

#### Answer

Sides of triangle are in ratio: 3:4:5

a = 3x, b = 4x, c = 5x

Since the perimeter of a triangle is given by:

a + b + c = perimeter

3x + 4x + 5x = 144

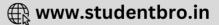
$$x = \frac{144}{12} = 12$$

$$x = 12$$

Therefore sides of the triangle are:

 $a = 3x = 3 \times 12 = 36,$  $b = 4x = 4 \times 12 = 48,$ 





 $c = 5x = 5 \times 12 = 60$ 

When a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

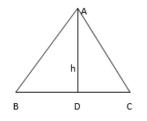
A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2} = \frac{36+48+60}{2} = 72$   
A =  $\sqrt{72(72-36)(72-48)(72-60)}$   
A =  $\sqrt{72\times36\times24\times12} = 864$  cm<sup>2</sup>

#### 7. Question

Find the area of an equilateral triangle having altitude h cm.

#### Answer

Let each side of equilateral triangle is a cm



Using pythagorous theorem in right  $\Delta ADB$ 

$$(AB)^{2} = (AD)^{2} + (BD)^{2}$$

$$(a)^{2} = (h)^{2} + (\frac{a}{2})^{2}$$

$$a = \frac{2h}{\sqrt{3}} \text{ cm}$$
Area of an equilateral triangle  $= \frac{\sqrt{3}a^{2}}{4} = \frac{\sqrt{3}\times 2h \times 2h}{4 \times \sqrt{3} \times \sqrt{3}} = \frac{\sqrt{3}k^{2}}{3} = \frac{\sqrt{3}k^{2}}{3 \times \sqrt{3}} = \frac{h^{2}}{\sqrt{3}} \text{ cm}^{2}$ 

4

#### 8. Question

Let  $\Delta$  be the area of a triangle. Find the area of a triangle whose each side is twice the side of the given triangle.

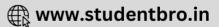
#### Answer

When each side of triangle = a

When a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

athte.

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2}$   
A' =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
When each side of triangle = 2a  
 $s' = \frac{2a+2b+2c}{2} = \frac{2(a+b+c)}{2} = 2s$   
A' =  $\sqrt{2s(2s-2a)(2s-2b)(2s-2c)}$   
A' =  $\sqrt{2s(2s-2a)(2s-2b)(2s-2c)} = 4\sqrt{s(s-a)(s-b)(s-c)} = 4A$   
9 Question



If each side of a triangle is doubled, then find percentage increase in its area.

#### Answer

Let the sides of triangle are a, b, c

When a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2}$   
A' =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula]

When each side of triangle is doubled

$$s' = \frac{2a+2b+2c}{2} = \frac{2(a+b+c)}{2} = 2 s$$
  
A' =  $\sqrt{2s(2s-2a)(2s-2b)(2s-2c)}$   
A' =  $\sqrt{2s(2s-2a)(2s-2b)(2s-2c)} = 4\sqrt{s(s-a)(s-b)(s-c)} = 4A$   
Increase in area =  $4A_{2}A_{3} = 3A_{3}$ 

Increase in area = 4A-A = 3A

Percentage increase in area =  $\frac{Inceased area}{Original area} \times 100 = \frac{3A}{A} \times 100 = 300\%$ 

#### 10. Question

If each side of an equilateral triangle is triples then what is the percentage increase in the area of the triangle?

#### Answer

When each side of triangle = a

Area of an equilateral triangle =  $\frac{\sqrt{3}a^2}{a}$  = A

When each side of triangle = 3a

Area of an equilateral triangle =  $\frac{\sqrt{3}(3a)^2}{a} = 9(\frac{\sqrt{3}a^2}{a}) = 9A$ 

Increase in area = 9A-A = 8A

Percentage increase in area =  $\frac{Inceased area}{Original area} \times 100 = \frac{8A}{A} \times 100 = 800\%$ 

#### 1. Question

The sides of a triangle are 16 cm, 30 cm, 34 cm. Its area is

A. 240 cm<sup>2</sup>

- B. 225 √₃ cm<sup>2</sup>
- C.  $225\sqrt{2}$  cm<sup>2</sup>
- D. 450 cm<sup>2</sup>

#### Answer

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

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A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]

*a* = 16, *b* = 30, *c* = 34

$$s = \frac{a+b+c}{2} = \frac{16+30+34}{2} = 40$$
  
A =  $\sqrt{40(40-16)(40-30)(40-34)}$   
A =  $\sqrt{40\times24\times10\times6} = 240 \text{ cm}^2$ 

## 2. Question

The base of an isosceles right triangle is 30 cm. Its area is

A. 225 cm<sup>2</sup>

B.  $225\sqrt{3}$  cm<sup>2</sup>

C.  $225\sqrt{2}$  cm<sup>2</sup>

D. 450 cm<sup>2</sup>

### Answer

Base = 30 cm, Altitude = 30 cm

Area of  $\Delta = \frac{1}{2}(Base \times Altitude)$ 

Area of  $\Delta = \frac{1}{2}(30 \times 30) = 450 \text{ cm}^2$ 

## 3. Question

The sides of a triangle are 7 cm, 9 cm and 14 cm. Its area is

A.  $12\sqrt{5}$  cm<sup>2</sup>

B. 12 √3 cm<sup>2</sup>

C. 24√₅ cm<sup>2</sup>

D. 63 cm<sup>2</sup>

### Answer

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  $a = 7 \ cm, b = 9 \ cm, c = 14 \ cm$  $s = \frac{a+b+c}{2} = \frac{7+9+14}{2} = 15$ 

$$A = \sqrt{15(15-7)(15-9)(15-14)}$$

### 4. Question

The sides of a triangular field are 325 m, 300 m and 125 m. Its area is

A. 18750 m<sup>2</sup>

B. 37500 m<sup>2</sup>

C. 97500 m<sup>2</sup>

D. 48750 m<sup>2</sup>

## Answer





Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $a = 325 m, b = 300 m, c = 125 m$   
 $s = \frac{a+b+c}{2} = \frac{325+300+125}{2} = 375$   
A =  $\sqrt{375(375-325)(375-300)(375-125)}$   
A =  $\sqrt{375\times50\times75\times250} = 18750 \text{ cm}^2$ 

#### 5. Question

The sides of a triangle are 50 cm, 78 cm and 112 cm. The smallest altitude is

- A. 20 cm
- B. 30 cm
- C. 40 cm
- D. 50 cm

#### Answer

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula] a = 50 cm, b = 78 cm, c = 112 cm  $s = \frac{a+b+c}{2} = \frac{50+78+112}{2} = 120$ A =  $\sqrt{120(120-50)(120-78)(120-112)}$ A =  $\sqrt{120\times70\times42\times8} = 1680 \text{ cm}^2$ Area of triangle =  $\frac{1}{2}$  (Base×Altitude)  $1680 = \frac{1}{2}$  (112×Altitude) Altitude = 30 cm

#### 6. Question

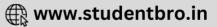
The sides of a triangle are 11 m, 60 m and 61 m. The altitude to the smallest side is

- A. 11 m
- B. 66 m
- C. 50 m
- D. 60 m

#### Answer

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $a = 11 m, b = 60 m, c = 61 m$   
 $s = \frac{a+b+c}{2} = \frac{11+60+61}{2} = 66$ 



 $A = \sqrt{66(66 - 11)(66 - 60)(66 - 61)}$ 

 $A = \sqrt{66 \times 55 \times 6 \times 5} = 330 \text{ m}^2$ 

Area of triangle =  $\frac{1}{2}(Base \times Altitude)$ 

 $330 = \frac{1}{2}(11 \times Altitude)$ 

Altitude = 60 m

## 7. Question

The sides of a triangle are 11 cm, 15 cm and 16 cm. The altitude to the largest side is

A. 30√7 cm

B.  $\frac{15\sqrt{7}}{2}$  cm

C. 
$$\frac{15\sqrt{7}}{4}$$
 cm

D. 30 cm

## Answer

Let a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

A =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula] a = 11 cm, b = 15 cm, c = 16 cm  $s = \frac{a+b+c}{2} = \frac{11+15+16}{2} = 21$ A =  $\sqrt{21(21-11)(21-15)(21-16)}$ A =  $\sqrt{21\times10\times6\times5} = \sqrt{3\times7\times2\times5\times2\times3\times5} = 30\sqrt{7} \text{ cm}^2$ Area of triangle =  $\frac{1}{2}$  (Base×Altitude)  $30\sqrt{7} = \frac{1}{2}$  (16×Altitude) Altitude =  $\frac{15\sqrt{7}}{4}$  cm

## 8. Question

If the area of an isosceles right triangle is 8 cm, what is the perimeter of the triangle?

A.  $8 + \sqrt{2}$  cm<sup>2</sup>

B.  $8+4\sqrt{2}$  cm<sup>2</sup>

C.  $4 + 8\sqrt{2}$  cm<sup>2</sup>

 $D.~12\sqrt{_2}~cm^2$ 

## Answer

In right isosceles  $\Delta ABC$ 

Area of triangle =  $\frac{1}{2}(Base \times Altitude)$ 

$$8 = \frac{1}{2}(x \times x) = \frac{1}{2}x^2$$

 $r = \sqrt{16} = 4 cm$ 





$$(AC)^{2} = (AB)^{2} + (BC)^{2}$$

$$y^{2} = x^{2} + x^{2}$$

$$A$$

$$A$$

$$A$$

$$B$$

$$x \text{ cm}$$

$$C$$

$$y^2 = 4^2 + 4^2$$

 $y^2 = \sqrt{4^2 + 4^2} = \sqrt{32} = 4\sqrt{2} \ cm$ 

Perimeter of  $\triangle ABC = AB + BC + CA = 4 + 4 + 4\sqrt{2} = 8 + 4\sqrt{2}$  cm

### 9. Question

The length of the sides of  $\triangle ABC$  are consecutive intergers. It  $\triangle ABC$  has the same perimeter as an equilateral triangle, triangle with a side of length 9 cm, what is the length of the shortest side of  $\triangle ABC$ ?

A. 4

B. 6

C. 8

D. 10

## Answer

Perimeter of an equilateral triangle with side 9 cm =  $9 \times 3 = 27$  cm

Let the sides of  $\triangle ABC$  are:  $AB = x_{x}BC = x + 1_{x}AC = x + 2$  (Since the sides of  $\triangle ABC$  are consecutive intergers)

Perimeter of  $\triangle ABC$  = Perimeter of equilateral triangle

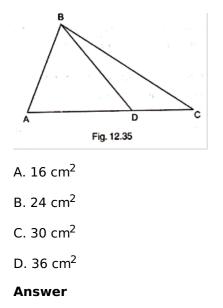
x + x + 1 + x + 2 = 27

3x = 27 - 3

x = 8 cm

### **10.** Question

In figure 12.35, the ratio of AD to DC is 3 to 2. If the area of  $\triangle ABC$  is 40 cm<sup>2</sup>, what is the area of  $\triangle BDC$ ?







In  $\triangle ABC$ AD:DC = 3:2 Area of  $\triangle ABD = \frac{1}{2}(Base \times Height) = \frac{1}{2}(AD \times Height)$ Area of  $\triangle BDC = \frac{1}{2}(DC \times Height) = \frac{1}{2}(DC \times Height)$   $\frac{area of \triangle ABD}{area of \triangle BDC} = \frac{\frac{1}{2}(AD \times Height)}{\frac{1}{2}(DC \times Height)} = \frac{AD}{DC} = \frac{3}{2}$ Area of  $\triangle ABC = \text{area of } \triangle ABD + \text{area of } \triangle BDC = 40 \text{ cm}^2$ 

3x + 2x = 40

5x = 40 = 8

Therefore area of  $\triangle ABD = 3x = 3 \times 8 = 24 \ cm^2$ 

Therefore area of  $\triangle BDC = 2x = 2 \times 8 = 16 \ cm^2$ 

### 11. Question

The base and hypotenuse of a right triangle are respectively 5 cm and 13 cm long. Its area is

A. 25 cm<sup>2</sup>

B. 28 cm<sup>2</sup>

- C. 30 cm<sup>2</sup>
- D. 40 cm<sup>2</sup>

## Answer

Using Pythagorous theorem:

 $(Hypotenuse)^2 = (Base)^2 + (Altitude)^2$ 

 $(13)^2 = 5^2 + (Altitude)^2$ 

 $(Altitude)^2 = 169 - 25 = 144$ 

Altitude = 12 cm

Area of triangle =  $\frac{1}{2}(5 \times 12) = 30 \ cm^2$ 

## 12. Question

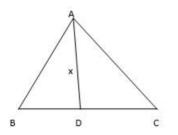
If the length of a median of an equilateral triangle is x cm, then its area is

A.  $x^2$ B.  $\frac{\sqrt{3}}{2} x^2$ C.  $\frac{x^2}{\sqrt{3}}$ D.  $\frac{x^2}{2}$ 









Median of an equilateral  $= \chi cm$ 

In an equilateral triangle median is an altitude.

Let the side of triangle be a cm

$$(AB)^{2} = (AD)^{2} + (BD)^{2}$$
  
 $(a)^{2} = (x)^{2} + (\frac{a}{2})^{2} C$   
 $a = \frac{2x}{\sqrt{3}} cm$ 

Area of an equilateral triangle  $= \frac{\sqrt{3}a^2}{4} = \frac{\sqrt{3}\times 2x \times 2x}{4 \times \sqrt{3} \times \sqrt{3}} = \frac{\sqrt{3}x\sqrt{3}x^2}{3} = \frac{\sqrt{3}\times \sqrt{3}x^2}{3 \times \sqrt{3}} = \frac{x^2}{\sqrt{3}} \text{ cm}^2$ 

### 13. Question

The length of each side of an equilateral triangle of area  $4\sqrt{_3}\,$  cm², is

A. 4cm

B. 
$$\frac{4}{\sqrt{3}}$$
 cm  
C.  $\frac{\sqrt{3}}{4}$  cm

D. 3 cm

#### Answer

Area of an equilateral triangle =  $4\sqrt{3}$  cm<sup>2</sup>

Let side of equilateral triangle = a cm

Area of an equilateral triangle =  $\frac{\sqrt{3}a^2}{4} = 4\sqrt{3}$ 

$$\Rightarrow a^2 = \frac{4 \times 4\sqrt{3}}{\sqrt{3}}$$

 $\Rightarrow a = 4 cm$ 

#### 14. Question

If every side of a triangle is doubled, then increase in the area of the triangle is

A.  $100\sqrt{2}$  %

B. 200%

C. 300%

D. 400%

### Answer

Let the sides of triangle are a, b, c

When a, b and c are the sides of triangle and s is the semi-perimeter, then its area is given by:

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A = 
$$\sqrt{s(s-a)(s-b)(s-c)}$$
 where  $s = \frac{a+b+c}{2}$  [Heron's Formula]  
 $s = \frac{a+b+c}{2}$   
A' =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s = \frac{a+b+c}{2}$  [Heron's Formula]

When each side of triangle is doubled

$$s' = \frac{2a+2b+2c}{2} = \frac{2(a+b+c)}{2} = 2s$$
  
A' =  $\sqrt{2s(2s-2a)(2s-2b)(2s-2c)}$   
A' =  $\sqrt{2s(2s-2a)(2s-2b)(2s-2c)} = 4\sqrt{s(s-a)(s-b)(s-c)} = 4A$ 

Increase in area = 4A-A = 3A

Percentage increase in area =  $\frac{Inceased area}{Original area} \times 100 = \frac{3A}{A} \times 100 = 300\%$ 

#### 15. Question

A square and an equilateral triangle have equal perimeters. If the diagonal of the square is  $12\sqrt{2}$  cm, then area of the triangle is

A.  $24\sqrt{2}$  cm<sup>2</sup>

B. 24√₃ cm<sup>2</sup>

C.  $48\sqrt{3}$  cm<sup>2</sup>

D.  $64\sqrt{3}$  cm<sup>2</sup>

### Answer

Let each side of square = y cm and each side of an equilateral triangle = x cm

Perimeter of square = perimeter of an equilateral triangle

4y = 3x .....(1)

Diagonal of square =  $12\sqrt{2}$  cm

Therefore using Pythagorous theorem:

$$y^2 + y^2 = (12\sqrt{2})^2$$

$$2y^2 = 288$$

$$y = 12 cm$$

Therefore substituting value of y in equation (1) we get: x = 16 cm

Area of an equilateral triangle =  $\frac{\sqrt{3}a^2}{4} = \frac{\sqrt{3}\times16\times16}{4} = 64\sqrt{3}cm^2$ 



